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AN UNDERSTANDING OF THE SHOULDER OF GIANTS: JOVIAN PLANETS AROUND LATE K DWARF STARS AND THE TREND WITH STELLAR MASS

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ABSTRACT

Analyses of exoplanet statistics suggest a trend of giant planet occurrence with host star mass, a clue to how planets like Jupiter form. One missing piece of the puzzle is the occurrence around late K dwarf stars (masses of $0.5 - 0.75M_{\odot}$ and effective temperatures of 3900–4800 K). We analyzed four years of Doppler radial velocities data of 110 late K dwarfs, one of which hosts two previously reported giant planets. We estimate that $4.0 \pm 2.3\%$ of these stars have Saturn-mass or larger planets with orbital periods < 245 d, depending on the planet mass distribution and RV variability of stars without giant planets. We also estimate that $0.7 \pm 0.5\%$ of similar stars observed by *Kepler* have giant planets. This *Kepler* rate is significantly (99% confidence) lower than that derived from our Doppler survey, but the difference vanishes if only the single Doppler system (HIP 57274) with completely resolved orbits is considered. The difference could also be explained by the exclusion of close binaries (without giant planets) from the Doppler but not *Kepler* surveys, the effect of long-period companions and stellar noise on the Doppler data, or an intrinsic difference between the two populations. Our estimates for late K dwarfs bridge those for solar-type stars and M dwarfs and support a positive trend with stellar mass. Small sample size precludes statements about finer structure, e.g. a “shoulder” in the distribution of giant planets with stellar mass. Future surveys such as the Next Generation Transit Survey and the Transiting Exoplanet Satellite Survey will ameliorate this deficiency.

Keywords: planetary systems — techniques: Doppler surveys, transit surveys

1. INTRODUCTION

Parent star mass is a fundamental parameter in planet discovery space because there are both theoretical predictions and observational evidence that the properties of planetary systems depends on central star mass. In addition, it is of practical significance: the sensitivity of the Doppler, astrometric, and transit techniques of planet detection scale inversely with stellar mass (or radius), such that smaller planets can be detected around less massive stars (or smaller) stars.

Most surveys for planets, i.e., ground-based radial velocity (RV) surveys and the *Kepler* transit survey mission, are flux- or magnitude-limited at visible wavelengths, favoring the inclusion of intrinsically bright stars. In addition, the Doppler method only works with spectra having large numbers of deep absorption lines, which disqualifies hot stars, and the transit method works better for cool dwarfs, around which planets produce deeper transits. These opposing trends mean that catalogs of exoplanet-hosting stars are dominated by solar-type stars with late F to early K spectral types

(Udry et al. 2007; Batalha et al. 2010). Moreover, a focus on solar-mass stars satisfies a desire to determine the occurrence, nature, and potential habitability of planets around other stars like the Sun.

On the other hand, M dwarf stars are now widely recognized as an attractive “short cut” to the discovery of Earth-like planets because such stars are numerous, small, and their habitable zones are close-in, meaning that planets orbiting within them will be more detectable by the Doppler or transit methods. Doppler surveys have included the few, nearby M dwarfs that are sufficiently bright at visible wavelengths (Bonfils et al. 2013), and high-precision infrared spectrographs are being constructed to take advantage of the greater emission of these stars at longer wavelengths (Artigau et al. 2011; Quirrenbach et al. 2012). Several thousand M dwarfs were added to the *Kepler* catalog for these reasons (Batalha et al. 2010).

Between the early K-type dwarfs and M dwarfs are the late K dwarfs, having K4–K7 spectral subtypes, $T_{\text{eff}} \approx 3900 - 4800$ K, and $M_{*} \approx 0.5 - 0.75M_{\odot}$. These stars have been comparatively neglected in planet surveys because they are intrinsically faint and because they are not M

dwarfs. The two largest Doppler surveys, the California Planet Search (CPS) and the HARPS survey, include relatively few late K stars. Ironically, these stars may be especially attractive targets for Doppler surveys because intrinsic stellar Doppler noise or “jitter” decreases with later spectral type and could be $< 1 \text{ m s}^{-1}$ among K dwarfs (Isaacson & Fischer 2010; Lovis et al. 2011). The K5 dwarf HD 85512 is one of the most Doppler-stable stars reported (residual RMS = 0.75 m s^{-1}), a property that has permitted the discovery of a super-Earth near or inside its habitable zone (Pepe et al. 2011).

Giant planets, defined here as planets with mass greater than that of Saturn ($95M_{\oplus}$) or radius greater than $8R_{\oplus}$, are readily detected by Doppler observations with a sufficient time baseline if the planets orbit within $\sim 1 \text{ AU}$ of their host stars. Their distribution with mass or spectral type of the host star can test the core accretion scenario of giant planet formation as well as models of orbital migration. Numerous studies have found evidence that the fraction of stars with giant planets increases with stellar mass (Fischer & Valenti 2005; Cumming et al. 2008; Johnson et al. 2010). Likewise, Fressin et al. (2013) estimated that the occurrence of giant planets is lower for *Kepler* M dwarfs than for G and K dwarfs. These findings support a theoretical prejudice that a more massive star is born with a more massive disk that can spawn the solid cores capable of accreting disk gas before its dispersal (Laughlin et al. 2004). However, any relation between disk mass and stellar mass is ambiguous (Williams & Cieza 2011). Moreover, the picture below $M_* = 0.75M_{\odot}$ is unclear because the statistics are poor; the sample of Johnson et al. (2010) included only 142 late K and M dwarfs with 5 reported giant planets. Likewise, the difference in giant planet occurrence around solar-type and M dwarf stars reported by Fressin et al. (2013) has only a 1.3σ significance. K dwarfs provide the “missing link” in this picture, and surveys for giant planets could reveal whether the difference in giant planet frequency exists, and whether it is a smooth transition or an abrupt “shoulder”.

The M2K Doppler survey targets the brightest late K dwarfs, bridging the gap between solar-type stars and M dwarfs. The survey reported one giant planet around an M3 dwarf (Apps et al. 2010) and a triple system including two Saturn- to Jupiter-mass planets around the K4-K5 dwarf HIP 57274 (GJ 439) with $T_{\text{eff}} \approx 4640 \pm 100\text{K}$ and $M_* \approx 0.73 \pm 0.05$, based on Yale-Yonsei isochrones (Fischer et al. 2012). Only four other mid- to late K-type dwarf hosts of giant planets have been reported: Jupiter-mass HAT-20b transits a similar K3 star with $T_{\text{eff}} \approx 4619 \pm 72\text{K}$ (Bakos et al. 2011a; Torres et al. 2012). The effective temperatures of the other three late K-type hosts (WASP-43b, HIP 70849, and WASP-80b) are not well established (Table 1 and Sec. 4.4). All other K dwarf hosts are hotter and have earlier spectral subtypes. We use the results of the M2K survey and *Kepler* to establish new constraints on the occurrence of giant planets around late K dwarfs and compare them with values for solar-type stars and M dwarfs.

2. METHODS: M2K SURVEY

2.1. Sample, Observations, and Reduction

Doppler observations were performed with the High Resolution Echelle Spectrograph (HIRES) on the Keck I telescope (Vogt et al. 1994). Observations obtained $R = 55,000$ with the B5 decker and a typical SNR of 200. Wavelength calibration was provided by a molecular iodine cell in the beamline. Radial velocity solutions were obtained by a forward modeling process in which an intrinsic stellar spectrum is obtained without the iodine cell, multiplied by a $R \sim 5 \times 10^5$ spectrum of the iodine cell taken with a Fourier Transform Spectrograph, and convolved by the instrumental profile. The relative shift in wavelength between the model and observed spectra is a free parameter. The median formal measurement error in the M2K survey is 1.25 m s^{-1} . We obtained $N = 4$ or more RV measurements on 159 stars. The median number of measurements for each star used in our analysis is $N = 9$, however the distribution of number of measurements is very uneven because of our strategy of follow-up of RV-variable stars (Fig. 1).

Ideally we would have defined our sample of late K dwarfs in terms of effective temperature T_{eff} , a fundamental stellar parameter, but not all our stars have spectroscopically-determined values. Thus we selected stars based on $V - J$ color as a proxy for T_{eff} . We restricted the sample to 140 stars with $1.8 < V - J < 2.8$, corresponding to $3900 < T_{\text{eff}} < 4750 \text{ K}$ or spectral subtypes K3-K7 (Gray & Corbally 2009), based on an empirical color- T_{eff} relation using stars with measured angular diameters (Boyajian et al. 2012). We corroborated this selection by estimating the T_{eff} of many of these stars using spectra (Fig. 2). Stellar parameters (including T_{eff} and metallicity $[\text{Fe}/\text{H}]$) of stars with $1.8 < V - J < 2.3$, were estimated using the Spectroscopy Made Easy package (Valenti & Piskunov 1996) (Table 2). SME performs poorly on dwarfs with $V - J > 2.3$ and $T_{\text{eff}} \leq 4300 \text{ K}$ so for these stars estimated T_{eff} by comparing moderate-resolution ($R \sim 1500$) visible-wavelength (3500-8500Å) spectra obtained with the Supernova Integral Field Spectrograph (Lantz et al. 2004) on the University of Hawaii 2.2 m telescope with synthetic spectra generated by the PHOENIX BT-SETTL program (Allard et al. 2011). The comparison procedure is described in Lépine et al. (2013) and was adjusted (Mann et al., in prep.) to maximize agreement with the calibrator stars of Boyajian et al. (2012). For stars without spectra, we estimated T_{eff} using $V - J$ color and the Boyajian et al. (2012) relation (Table 2).

The median offset between SME-derived and $V - J$ -based temperatures is 140 K. For this reason, we included the 13 stars with SME-based $T_{\text{eff}} > 4750 \text{ K}$ (but acceptable $V - J$) as their actual effective temperatures are probably within the acceptable range. Unsurprisingly, T_{eff} estimates based on calibrated comparisons between moderate-resolution spectra and PHOENIX models are consistent with the Boyajian et al. (2012) relation. Nearly all of our stars have measured parallaxes and we estimated masses using the relation with absolute K magnitude in Henry & McCarthy (1993). For those few stars lacking parallaxes we used the empirical relations between T_{eff} , stellar radius, and stellar mass in Boyajian et al. (2012).

We excluded stars exhibiting relatively high emission in the H and K lines of Ca II. These stars are chromo-

spherically active and tend to exhibit higher astrophysical Doppler noise or “jitter” (e.g. Isaacson & Fischer 2010). Figure 3 shows values of S_{HK} , the flux in the Ca II line cores normalized by the continuum, vs. $V - J$ color. The trend of increasing S_{HK} with redder $V - J$ is due to the lower blue continuum rather than elevated Ca II emission, in redder stars. We calculated a running median ($N = 20$), fit a linear function \bar{S}_{HK} with $V - J$, and subtracted that from these values. The histogram (inset of Fig. 3) suggests a cutoff at $S_{HK} - \bar{S}_{HK} = 0.44$, which rejects 11 stars as exceptionally active. Among the stars we admitted were 5 for which it was not possible to estimate S_{HK} because the continuum was not detected.

We next considered the distribution of RV standard deviations (RMS) of the remaining 129 stars. The majority (100) of the stars fall in a cluster with $\text{RMS} < 15 \text{ m s}^{-1}$ (Fig. 4). We inspected the RV data of the 29 stars with $\text{RMS} > 15 \text{ m s}^{-1}$. One of these is HIP 57274, which has been described elsewhere (Fischer et al. 2012). Eight others have additional stars within 5 arc sec and were excluded because leakage of light into the spectrograph slit is an established source of RV error.

We analyzed each of the remaining 20 sets of RVs with both weighted linear and quadratic regressions and applied an F-test to evaluate the significance of any reduction in variation after subtraction of the fit. Although all stars have ≥ 4 RV measurements, and thus the number of degrees of freedom for a quadratic fit is ≥ 1 , irregular sampling means that over-fitting and erroneous reduction in RV variation is possible. For example, four observations in two very closely-spaced pairs cannot be reliably regressed: a significant radial velocity offset between the pairs could be the result of a linear trend or any RV variation. To identify such cases, we computed an effective N equal to the sum of normalized Voronoi-type weights $w_i = (t_{i+1} - t_{i-1})/2$ that are often assigned by regularization algorithms (Strohmer 2000). End points have weights $w_1 = t_2 - t_1$ and $w_N = t_N - t_{N-1}$. Thus

$$N_{\text{eff}} = \frac{3(t_N - t_1) - (t_{N-1} - t_2)}{2 \max(w_i)}. \quad (1)$$

In the limit of large N , N_{eff} and thus the maximum order of the polynomial that should be used in a regression approach the total time interval divided by the maximum interval between points. This is analogous to the Nyquist sampling criterion.

Doppler datasets with $\text{RMS} > 15 \text{ m s}^{-1}$ were processed in one of three ways: (i) If regressions did not significantly reduce variance (F-test $p < 0.05$) the data were analyzed as is. (ii) If a regression did significantly reduce variance and N_{eff} was > 3 (or > 4 , in the case of a quadratic), the best fit is subtracted before analysis. (iii) If a regression is significant but N_{eff} is not sufficiently large, the star and its data were excluded from the analysis. We excluded 11 stars in this way, leaving 110 stars for analysis, including HIP 57274.

HIP 2247 has a long-period super-Jupiter previously identified by Moutou et al. (2009). We fit the combined HARPS and Keck-HIRES data using the RVLIN code (Wright & Howard 2009), generating errors using 100 Monte Carlo realizations of the data by randomly reshuffling the residuals to the previous fit. We find essentially the same planetary parameters as Moutou et al. (2009),

but with significantly reduced uncertainties: $M_p \sin i = 5.14 \pm 0.02 M_J$, $P = 655.90 \pm 0.22 \text{ d}$, and $e = 0.543 \pm 0.0011$, with a residual RMS of 3.8 m s^{-1} (Fig. 5). No significant trend was found ($-0.0024 \pm 0.0011 \text{ m s}^{-1}$). The uncertainty in $m \sin i$ does not include errors in the estimated stellar mass of $0.77 M_\odot$. Any giant planets with $P < 245 \text{ d}$ can be ruled out: we include this system in our sample but consider it a definitive non-detection.

HIP 38117 exhibits RV variation consistent with the presence of a stellar-mass companion on a $81.28 \pm 0.01 \text{ d}$ orbit with an eccentricity of 0.478 ± 0.012 (Fig. 6). Assuming a primary mass of $0.73 M_\odot$ based on the system’s $V - J$ color, and assuming that the secondary contributes negligible flux, the companion’s $M_* \sin i$ is $0.45 \pm 0.16 M_\odot$, i.e. this is a very late K or M dwarf. (This calculation assumes an average value of $\langle \sin i \rangle = \pi/4$ to calculate the total system mass.) The residual RMS is 3 m s^{-1} ($N = 15$). As a planetary orbit with a comparable orbital period is unlikely to be stable, we follow the suit of other studies by excluding this binary system from our analysis.

2.2. Estimation of Planet Fraction

We estimated the fraction of stars f with giant planets having $M_P > 0.3 M_J$ (i.e. Saturn mass) and Keplerian orbital periods $1.7 \text{ d} < P_K < 245 \text{ d}$. The choice of outer cutoff in P_K is based on the temporal baseline of our data - nearly all stars were monitored for at least 245 d - and motivated by the longest bin with good statistics in the analysis of *Kepler* planet candidates by Fressin et al. (2013). The inner cutoff corresponds to the location of the rollover in the period distribution of giant planets around *Kepler* stars (Howard et al. 2012). We construct and maximize a likelihood function to find the most probable value of f and its uncertainty. The details of the calculations are given in the Appendix and the method is only summarized here.

A standard procedure to estimate the fraction of stars with planets is to maximize a binomial expression involving the product of detections and non-detections. However, with RV data it can be difficult or impossible to rule out all possible planets, e.g. those on face-on orbits. Thus we replace detections and non-detections with a Bayesian statistic that is sum of the probabilities p_i^0 and p_i^1 that there are zero or one giant planets around the i th star, with $1 - f$ and f as *priors* for zero or one planets, respectively:

$$\ln \mathcal{L} = \sum_i \ln (p_i^0 (1 - f) + p_i^1 f), \quad (2)$$

where the sum is over all stars. This counts multi-giant planet systems once, and thus underestimates the planet *occurrence* (planets per star). The probabilities p_i^0 and p_i^1 are Gaussian functions of the difference between the predicted and observed radial velocities v_{ij} and \hat{v}_{ij} , weighted by priors \tilde{p}_i marginalized over all model parameters

$$p_i^n = \langle \tilde{p}_i \exp \left[- \sum_j \frac{(v_{ij} - \hat{v}_{ij}^n)^2}{2\sigma_{ij}^2} \right] \rangle, \quad (3)$$

and where σ_{ij} are the formal errors, astrophysical noise or “jitter”, as well as systematic error and the contribution of small planets to motion of the star around the

system’s barycenter (see Sec. 4.1), added in quadrature. This method is analogous to the approach used in Gaidos et al. (2012) but uses the individual RV measurements, not the RMS.

The Gaussian form of Eqn. 3 means that only the best-fit sets of parameter values (barycenter motion v_0 , Keplerian period P_K , Doppler amplitude K , eccentricity e , longitude of periastron ω and time of periastron t_0) make significant contributions to p^0 or p^1 . We used the linear dependence of the radial velocities on the barycenter velocity v_0 and Doppler amplitude K to analytically solve for the best-fit values of these two parameters given values for the other parameters. To marginalize over planet mass we used the relation between K , planet mass, and orbital inclination and adopt a power-law distribution of log mass with an index $\alpha = -0.31$ (Cumming et al. 2008). (The sensitivity of our results to this value is explored in Section 4.2.) We marginalized Eqn. 3 over the full range of possible values of e , ω , t_0 , using a Rayleigh function for the prior on eccentricity (Moorhead et al. 2011) and uniform priors for ω and t_0 . We further evaluated the probability over $3 \text{ d} < P_K < 245 \text{ d}$ at intervals of equal prior probability, assuming a power-law distribution for log period having index $\beta = 0.26$ (Cumming et al. 2008). To better sample intervals of P_K corresponding to higher probability we used each P_K value as an initial value in a fit of a Keplerian solution to the data with the RVLIN routine (Wright & Howard 2009). We used the fixed, best-fit values of the other parameters for the RVLIN fit, obtained an adjusted value of P_K , and then re-calculated the other parameters as described above. This procedure was repeated two times, which we found was sufficient for convergence.

We calculated p^0 and p^1 by summing over final values of all the parameters, and normalizing by $p^0 + p^1$. For three stars p_0 and p_1 were both incalculably small due to large disagreements between v and \hat{v} for either the zero- or one-planet models. This could be due to elevated stellar jitter or the presence of smaller planets (see below). For these stars we assigned $p_0 = p_1 = 0.5$, i.e. the zero- and one-planet models are accepted or rejected with equal likelihood. We then evaluated Eqn. 2 over all possible values of f , and found the maximum. We calculated an approximate uncertainty by assuming asymptotic normality, iteratively fitting a parabola to the log-likelihood curve, and assigning $\sigma_f = 1/\sqrt{2C}$, where C is the curvature coefficient of the parabola.

Both the zero- and one-planet models do not account for barycenter motion due to the presence of other, smaller planets, as well as any sources of systematic error. As a result, for some stars both models are strongly rejected, leading to an erroneously high value of f . To account for this effect, we treat this barycenter motion as an additional source of uncorrelated, random RV noise or “jitter” that, along with stellar noise, can be described by a single value of σ_0 . A value for σ_0 was chosen by assuming that the pronounced cluster of systems with $\text{RMS} < 15 \text{ m s}^{-1}$ (Fig. 4) represents stars without giant planets, and fitting that distribution by a Monte Carlo model. We constructed 1000 artificial realizations of the data with the same number of RVs per star but drawn from a random normal distribution. The variance of this distribution was set equal to the formal measurement error

and a trial value of σ_0 added in quadrature. We computed the RMS values and comparing the distribution to the observed distribution (after subtracting any trends) with a two-sided Kolmogorov-Smirnov test. We found that a curve with $\sigma_0 = 6.3 \text{ m s}^{-1}$ (solid curve in Fig. 4) maximizes the K-S probability of the Monte Carlo distribution (inset of Fig. 4), and we use that value in our estimation of f . The poor agreement between the observed and “best-fit” distributions reflects the inability of a single value of σ_0 to capture the diversity of stellar RV behavior.

3. METHODS: KEPLER SURVEY

We compared our estimate of the fraction of M2K dwarfs with giant planets with one for late K dwarfs observed by *Kepler*. We selected *Kepler* targets with $1.8 < V - J < 2.8$, with V magnitudes estimated using the relation $V = r + 0.44(g - r) - 0.02$ (Fukugita et al. 1996). We further limited the sample to stars that had been observed in at least seven of quarters Q1-Q8. The absence of a single quarter will minimally affect the detection efficiency but is common because some stars were added after Q1 and others fall within *Kepler*’s defunct CCD module during one of four rotations of the spacecraft. Stellar and planetary parameters of *Kepler* stars were estimated by fits to Dartmouth stellar models (Dotter et al. 2008) using the Bayesian procedure described in Gaidos (2013). We restricted the analysis to 6293 dwarf stars with $3900 < T_{\text{eff}} < 4800 \text{ K}$, $\log g > 4$, and $K_P < 16$. In this sample are two giant planet candidates with $P_K < 245 \text{ d}$: KOI 1176.01 is a hot Jupiter ($P_K = 1.94 \text{ d}$) orbiting a star with $T_{\text{eff}} \approx 4625 \text{ K}$. The second (KOI 868.01) has an orbital period of 235.9 d. Another giant planet candidate (KOI 1466.01) has $P_K = 281.6 \text{ d}$ and was excluded, and a fourth (KOI 1552.01) was excluded from our sample because *Kepler* observed it for only five of the eight quarters.

Following Mann et al. (2012), we calculated the binomial log likelihood for a flat log distribution with period and a monotonic radius distribution in the limit that the transit probability is low:

$$\ln \mathcal{L} = \sum_i^D [\ln f + \ln D_i(P_i)] - \frac{f}{\ln(P_2/P_1)} \sum_j^{ND} F_j, \quad (4)$$

where the orbital period range is $P_1 < P_K < P_2$, the two summations are over detections and non-detections, respectively, $D_i(P)$ is the probability of detecting a planet around the i th star,

$$F_j = \int_{P_1}^{P_2} D_j(P) d \ln P, \quad (5)$$

and an uninteresting constant is ignored. To compare with the M2K results we use $P_1 = 1.7 \text{ d}$ and $P_2 = 245 \text{ d}$.

We assumed that any transit of a giant planet in front of a late K dwarf will be detected. The typical transit depth is ~ 0.02 , which is far larger than the noise: The median 3 hr Combined Differential Photometry Precision for these stars is 1.8×10^{-4} and the 99% value of 6.6×10^{-4} , corresponding to SNR of ~ 110 and 30, respectively. Fressin et al. (2013) found that the recovery rate of the *Kepler* detection pipeline was nearly 100% for $\text{SNR} > 16$.

Thus the detection probability is simply the geometric factor R_*/a , where a is the orbital semimajor axis, and

$$D_j(P) = \left(\frac{4\pi^2 R_*^3}{GM_*} \right)^{1/3} \frac{1 + e \cos \omega}{1 - e^2} P_K^{-2/3} \quad (6)$$

We marginalized F (Eqn. 5) over e and ω and adopted a distribution $n(e)$ for eccentricity. Ignoring terms that do not depend on f , Eqn. 4 becomes

$$\ln \mathcal{L} \approx N_D \ln f - 0.356 f \left[\int_0^1 \frac{n(e)de}{1 - e^2} \right] \left(\frac{P_2}{1 \text{ d}} \right)^{-2/3} \times \frac{(P_2/P_1)^{2/3} - 1}{\ln(P_2/P_1)} \sum_j^{N_D} \left(\frac{\rho_j}{\rho_\odot} \right)^{-1/3}, \quad (7)$$

where N_D is the number of detected planets and ρ is the mean density of the star. Adopting the function for $n(e)$ in Shen & Turner (2008), we found that the integral is only weakly dependent on the parameter a in their distribution, and is ≈ 1.20 for $a = 4$. Using a Rayleigh distribution like that for the M2K analysis gives a similar value (1.08) for the integral. Because each star can be explained by more than one stellar model with probability p , we used a weighted mean of $\rho^{-1/3}$ to calculate the likelihood:

$$\langle \rho^{-1/3} \rangle = \sum_i p_i \rho_i^{-1/3} / \sum_i p_i, \quad (8)$$

where the summation is restricted to main sequence models, i.e. $\log g > 4$.

We compared our analysis with that of Howard et al. (2012) by calculating f for dwarfs with $4100 < T_{\text{eff}} < 4600$ K and $4600 < T_{\text{eff}} < 5100$ K, and restricting the period range to $0.68 \text{ d} < P_K < 50 \text{ d}$. Our results are 0 and 0.3% for the respective T_{eff} bins, compared to 0 and $2.7^{+1.0}_{-1.4}\%$ from Howard et al. (2012). Despite the same restrictions on T_{eff} , there are differences in the samples because we reclassified some K stars as giants (and any candidate giant planets as stellar companions) and we imposed a V - J color cut which excludes many systems from the hotter T_{eff} bin, whereas Howard et al. (2012) required $K_P < 15$.

4. RESULTS AND DISCUSSION

4.1. Fraction of Stars with Giant Planets

Values of p^1 , the probability that the RV data are consistent with the presence of a giant planet with $P_K < 245 \text{ d}$, are reported for the 110 late K dwarfs in Table 2 (note that $p^0 = 1 - p^1$). Figure 7 shows the relative likelihood distribution of f constructed from these values using Eqn. 2. The most probable value of f is 4.0% and the uncertainty based on the assumption of asymptotic normality is $\pm 2.3\%$. The elevated range relative to the rate of actual detections (1 of 110 stars) is due to the presence of several stars in our sample with significantly non-zero values of p^1 . Eighteen stars have $p^1 > 0.2$ and four, excluding HIP 57274, have $p^1 > 0.9$ (Table 2). We are continuing to monitor these stars (Boyajian et al., in prep.). If we assume that giant planets with $P_K < 245 \text{ d}$ are ruled out ($p^1 = 0$) for all stars other than HIP 57274 (the “HIP 57274 only” case in Fig. 7), the most probable value of f becomes $0.92 \pm 0.75\%$.

Stars may exhibit high RV variation for reasons other than the presence of giant planets with $P < 245 \text{ d}$. Many M2K target stars were monitored for intervals $\gg 245 \text{ d}$ and our RV data is sensitive to the presence of planets on wider orbits. Both Doppler and *Kepler* surveys find such planets, e.g. HIP 2247 and KOI 1466.01 (see below). Some stars may have a lower-mass (M dwarf) companion like that of HIP 38117 (Fig. 6), but on a wider orbit. If the trend in RV produced by such a companion isn’t resolved because of undersampling, it will manifest itself as a high RMS. Despite our precautionary elimination of stars with Ca II HK emission, some stars in our sample may have high intrinsic “jitter” from spots. Many stars in our sample have only a few Doppler observations (Fig. 1), confounding these effects. Ultimately, additional observations are required to discriminate between these possibilities.

The relative likelihood distribution of f for late K dwarfs observed by *Kepler* is plotted as the dashed line in Fig. 7. The most likely value of f is $0.7 \pm 0.5\%$. Based on the two distributions, we calculate a 99% probability that the *Kepler* value is actually lower than the M2K value. Due to the factors discussed above, the M2K value of 4% may be an overestimate: There is a closer correspondence (85% chance that the *Kepler* estimate is lower) if we rule out giant planets around all stars other than HIP 57274. Wright et al. (2012) report that the occurrence of “hot” Jupiters around the FGK stars in the California Planet Search Doppler survey is 1.2%, compared to 0.4% for *Kepler* (Howard et al. 2012; Fressin et al. 2013). Gaidos & Mann (2013) proposed that the difference between the transit and Doppler results may be due the presence of subgiants in the *Kepler* target catalog: planets around such stars will be more difficult to detect and more likely to experience destructive orbital decay. This explanation may be less applicable to late K spectral types where the giant and main sequence branches are more distinguishable, and we consider orbits with $P_K \gg 10 \text{ d}$ on which orbital decay will be negligible. Another explanation for at least some of this difference is the exclusion of spectroscopic and resolved binaries from the M2K sample, but not the *Kepler* sample, may enrich for giant planets, presuming that such binaries are less likely to host planets for dynamical reasons (e.g., Thébault et al. 2006; Bonavita & Desidera 2007; Kaib et al. 2013).

We compare our M2K and *Kepler* estimates of f for late K dwarfs with previous studies for different ranges of stellar mass (Fig. 8). Our estimates bridge the gap between solar-type stars (Fischer & Valenti 2005; Cumming et al. 2008; Johnson et al. 2010; Howard et al. 2010, 2012; Fressin et al. 2013) and M dwarfs (Naef et al. 2005; Cumming et al. 2008; Johnson et al. 2010; Bonfils et al. 2013; Fressin et al. 2013). We have adjusted values by the factor $\ln(P_{\text{max}}/1.7 \text{ d})/\ln(245/1.7)$ to account for differences in the maximum orbital period P_{max} of each survey, assuming a flat distribution with $\ln P_K$. (The adjustment is not sensitive to the exact distribution assumed.) The surveys also differ somewhat in the mass or radius ranges of objects counted as giant planets. For example, although our *Kepler*-based estimate of 0.7% for late K dwarfs seems much lower than those of Fressin et al. (2013) for either GK dwarfs ($6.1 \pm 0.9\%$) or M dwarfs ($3.6 \pm 1.7\%$), these statistics

are for $P_K < 418$ d rather than 245 d, and $R_p > 6R_\oplus$, rather than the $8R_\oplus$ convention adopted here. Their overall f falls to 4.1% for $P < 245$ d, and our f rises to $1.1 \pm 0.6\%$ if we include planets with $R_p > 6R_\oplus$, bringing these two figures closer. Taken together, these estimates suggest an overall trend, perhaps linear, of increasing giant planet occurrence with stellar mass, there is not yet any indication of finer structure. A linear least-squares of the adjusted Doppler data yields $f(\%) = -1.11 + 5.33 M_*/M_\odot$ (dashed line in Fig. 8) with weak significance (F -test probability of 0.12). This compilation also suggests that the deficit of giant planets around *Kepler* stars relative to the targets of Doppler surveys (Wright et al. 2012) depends on host star mass (Fig. 8), although clearly a more homogeneous analysis of the collective data sets is needed.

A correlation between giant planets and the metallicity of the host star has been unambiguously established for solar-type stars (e.g., Fischer & Valenti 2005), and is strongly supported by the available evidence for M dwarfs (Neves et al. 2013; Mann et al. 2013). The median metallicity of our sample of late K dwarfs is solar ($[\text{Fe}/\text{H}] = 0.004$). The metallicities of HIP 57274 and HIP 2247, the two stars known to host giant planets in our sample, are 0.08 and 0.24 dex, consistent with this trend. The difference in the distributions of metallicities of stars with $p^1 < 0.1$ (median $[\text{Fe}/\text{H}]$ of -0.01) and those with $p^1 > 0.1$ (median $[\text{Fe}/\text{H}]$ of 0.08) is marginally significant (K-S probability of 0.06), further supporting a giant planet-metallicity relation in late K dwarfs. If SME overestimates the T_{eff} of these stars (Fig. 2), the $[\text{Fe}/\text{H}]$ is also overestimated by about 0.1 dex per 100 K.

4.2. Sensitivity to Parameter Values

Our estimates of f may be sensitive to the values of any one of several parameters we use in our calculations (see Appendix). These include the computational resolution n with which p_i^N is evaluated over ranges of the various orbital parameters, the power-law indices α and β for the assumed mass and period distributions, the mean value \bar{e} of the Rayleigh-distributed eccentricities, and the RV jitter σ_0 which is assumed for each star. Due to the computational requirements of such studies, we first considered the effect on two stars, HIP 37798 and HIP 66074, with number of observations equal to the median ($N = 9$) but with the smallest (0.005) and large (0.82) values of p^1 , respectively. Based on the outcome sensitivity of p^1 to varying parameter values, we selectively investigated the effects on our estimates of f .

Varying n from 25 to 50 (at rapidly increasing computational cost) had a negligible effect on p^1 for HIP 37798 but decreased the value for HIP 66074 by about 13%. We found that p^1 varied little for $n > 50$. Thus we re-analyzed 17 stars with p^1 values > 0.2 (excluding HIP 57274) using $n = 50$. Not all stars were re-analyzed because of the high computational cost. These $n = 50$ values are used in the calculations of f in Section 4.1. Without the substitution of high-resolution values, the most likely value of f is $5.1 \pm 2.7\%$.

We varied the power-law index α of the planet mass distribution by ± 0.2 from its nominal value of -0.31 based on Cumming et al. (2008) (see also Howard et al. 2012). p^1 increased significantly and systematically with more

negative values of α , by a factor of 3.5 for HIP 37798 and nearly 1.5 for HIP 66074. We found that the most probable value of f changed from 3% to 6.4% when we varied α from -0.11 to -0.51. Also based on Cumming et al. (2008), we varied the power-law index β of the orbital period distribution by ± 0.1 from its nominal value of 0.26. We found that the p^1 for HIP 37798 was essentially unchanged, while that of HIP 66074 changed by only $\pm 15\%$. Varying \bar{e} by ± 0.1 from its nominal value of 0.225 (Moorhead et al. 2011) also had a negligible effect on the p^1 of HIP 37798 and changed that of HIP 66074 only slightly. Thus our estimate of f is not sensitive to the assumed distributions of orbital period and eccentricity, but does depend on the mass distribution. The last occurs because a steeper mass function (more negative α) includes more Saturn-mass planets that could be hidden on low inclination orbits in our RV data.

Finally, we varied the value of σ_0 assigned to each star to account for astrophysical noise and barycenter motion induced by small planets. We considered a range of 6-6.75 m s^{-1} based on where the K-S probability that the observed and simulated RV RMS distributions are within a factor of 0.05 (i.e. 95% confidence) of the maximum at $\sigma_0 = 6.3 \text{ m s}^{-1}$ (see Sec. 2.2). For both stars, values of p^1 increase significantly if σ_0 is decreased from its nominal value, but increased only slightly for higher σ_0 . Correspondingly, f increased by a factor of 1.6 for $\sigma_0 = 6 \text{ m s}^{-1}$, and decreased by 0.82 for $\sigma_0 = 6.8 \text{ m s}^{-1}$. A smaller σ_0 means that the more RV variation must be explained by the presence of giant planets, e.g., Saturn-mass planets with low orbital inclinations.

4.3. Implications for theory

A correlations between the occurrence of giant planets and stellar metallicity (e.g., Fischer & Valenti 2005; Johnson et al. 2010) has been interpreted as supporting the core accretion scenario of giant planet formation. In that scenario, growth of a sufficiently massive solid core leads to the runaway accretion of gas, but only if it occurs before the gas disk is dissipated in a few million years (Lissauer & Stevenson 2007). In disks of higher metallicity gas, dust grains can grow, collide, and settle to the mid-plane more rapidly, thus initiating planet formation at an earlier epoch (Johnson & Li 2012). Simulations of rocky planet mass by Kokubo et al. (2006) produced a linear trend between final planet mass and initial disk mass surface density. Thus, disks around high-metallicity disks should produce larger rocky cores around which gas could accrete more quickly.

However, a trend with stellar mass, supported by our results, may require a more complex explanation. First, the dependence of disk mass on stellar mass appears to be weak (Williams & Cieza 2011) and higher disk mass need not translate into higher mass surface density – and more massive planets (Kokubo et al. 2006) – if the radial extent of the disk is larger. Moreover, Doppler and transit surveys of FGK stars thoroughly probe orbital semimajor axes to $\lesssim 1$ AU; available radial velocity data suggest a “jump” in the population of giant planets just beyond 1 AU (Wright & Howard 2009) and set generous lower limits on their occurrence on much wider orbits (e.g., Wittenmyer et al. 2011). Microlensing surveys suggest that as many as a third of lensing stars

(typically late K and M dwarfs) host giant planets at 1-5 AU (Mann et al. 2010; Cassan et al. 2012). If giant planet formation preferentially occurs on these orbits, the correlation with stellar mass may arise from varying efficiency of inward migration, rather than formation, of giant planets.

4.4. *On the shoulder of giants*

The coolest giant planet host stars in our M2K and *Kepler* samples are HIP 57274 and KOI 1176.01 with temperatures of 4640 K and 4625 K. The only cooler K dwarfs hosting reported giant planets are WASP-43, HIP 70849, and WASP-80 (Table 1), but only the WASP planets are on close-in orbits. The effective temperature of WASP-43, based on the shape of the Balmer H α line, is 4400 K (Hellier et al. 2011), and this is broadly consistent with the $V - J$ color of 2.4. However, this star is active and chromospheric emission may fill in and weaken the H α line, making the temperature estimate erroneously low. An analysis of transit light curves coupled with stellar models suggests 4520 ± 120 K instead (Gillon et al. 2012). The T_{eff} assigned to HIP 70849 was based solely on its luminosity and a theoretical temperature-luminosity relation (Ségransan et al. 2011). WASP-80 shares spectral characteristics with both K7 and M0 dwarfs and analyses of a spectrum and infrared photometry suggests temperatures of 4145 ± 100 and 4020 ± 130 K, respectively (Triaud et al. 2013).

Depending on the properties of WASP-43 and WASP-80, these stars may bracket a T_{eff} range of 4100-4600 K over which giant planets on close orbits have yet to be found. This could be a hint of structure, i.e a gap or “shoulder” in the giant planet distribution with stellar mass, but any conclusion require new surveys. Giant planets appear to orbit at wider separations around such stars (e.g., HIP 70849b and KOI 868.01), and future space-based astrometric searches with the *Gaia* mission (de Bruijne 2012) and microlensing surveys by *Euclid* (Penny et al. 2012) or the proposed WFIRST observatory (Barry et al. 2011) should reveal such planet populations in detail.

We have used the M2K and *Kepler* surveys to place approximate constraints on the fraction of late K dwarfs with giant planets, but the target catalogs are of inadequate size to address the question of any “fine structure” in the distribution of giant planets with stellar mass. The Next Generation Transit Survey (www.ngtransits.org) will monitor 40,000 late G- to early M-type stars to search for “hot” Neptunes. Based on our inferred occurrence rate we expect there to be ~ 10 Jupiters around these target stars, however most of these will have orbital periods > 10 d where the detection efficiency of a ground-based survey at a single site like NGST is low. The Transiting Exoplanet Survey Satellite will survey ~ 2.5 million stars to $V = 13$ (Deming et al. 2009) and, according to the TRILEGAL stellar model of the Galaxy (Girardi et al. 2012), approximately 50,000 targets will be late K dwarfs with $4000 < T_{\text{eff}} < 4800$ K. Monitoring of these should significantly improve the statistics and allow us to see further.

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APPENDIX

LIKELIHOOD ESTIMATION OF PLANET OCCURRENCE

In a survey where any giant planet (within the allowed orbital period range) would be detected, and non-detections unambiguously rule out planets, the fraction of stars with giant planets f can be calculated by maximizing the binomial probability distribution for D detections among N systems,

$$P = \frac{N!}{D!(N-D)!} f^D (1-f)^{N-D}. \quad (\text{A1})$$

The first factor can be ignored because it does not depend on f , allowing the problem to be translated into maximizing a log likelihood:

$$\log \mathcal{L} = D \log f + (N-D) \log(1-f). \quad (\text{A2})$$

However, most of our RV data are ambiguous in that they are neither detections nor can they rule out all possible giant planets. Specifically, they can only exclude planets of a certain minimum mass or minimum inclination with certain combinations of other orbital parameters.

Equation A2 can be generalized to $\log L = \sum_i \log \ell_i(f)$, where $\ell_i(f)$ is the probability that the RV data of the i th star can be explained by a value of f . Further, the parameter f describes the underlying probability distribution for the presence or absence of a giant planet, which in turn generates a model of the RV data. Using an empirical Bayes/marginalized likelihood approach this is expressed as a posterior probability

$$\ell_i(f) = \sum_{N=0}^1 p(D_i|M_N) q(M_N|f), \quad (\text{A3})$$

where $p(D_i|M_N)$ is the probability that the i th RV data set can be explained by a model M_N with N planets, $q(M_N|f)$ is the prior probability of M_N given f , and the likelihood is marginalized over the number of planets. We seek the value of the “hyperparameter” f that maximizes

$$\log \mathcal{L} = \sum_i \log [p_i^0(1-f) + p_i^1 f], \quad (\text{A4})$$

where $p_i^N = p(D_i|M_N)$ marginalized over all other model parameters. Because we expect f to be $\ll 1$, we neglect multiple-giant planet models.

Assuming Gaussian errors in RV,

$$p_i^n = \exp \left[- \sum_j \frac{(v_j - \hat{v}_j^n)^2}{2\sigma_j^2} \right] \tilde{p}, \quad (\text{A5})$$

where v_j are the RV measurements, \hat{v}_j^n are the model values for $n = 0$ or 1 exoplanets, σ_j are the errors, and \tilde{p} represents the product of priors on the model parameters.

The radial velocity model \hat{v}_j of a single planet around a star depends on six parameters: barycenter velocity v_0 , $M_p \sin i$, where i is the inclination, orbital period P_K , eccentricity e , argument of periastron ω , and epoch of zero true anomaly t_0 . We express this as $\hat{v}_j = v_0 + K g(t_j)$, where K is the amplitude of the reflex motion,

$$g(t_j) \equiv \cos(\nu_j(t_j) + \omega) + e \cos \omega, \quad (\text{A6})$$

and ν_j is the true anomaly of the planet at epoch t_j . In the limit where $M_p \ll M_*$ the reflex amplitude is

$$K = \frac{M_p \sin i}{M_* \sqrt{1-e^2}} \left(\frac{2\pi G M_*}{P_K} \right)^{1/3}. \quad (\text{A7})$$

The true anomaly is found by solving for the eccentric and mean anomalies η and μ ,

$$\cos \nu = \frac{\cos \eta - e}{1 - e \cos \eta}, \quad (\text{A8})$$

$$\mu = \eta - e \sin \eta, \quad (\text{A9})$$

and

$$\mu = \frac{2\pi}{P} (t_j - t_0). \quad (\text{A10})$$

In the single planet model $\hat{v}_j = v_0$, which is the only parameter in this case.

A precise calculation of p_i^N must marginalize over all possible parameter values weighted by \tilde{p} . This is computationally expensive, but if $\sigma \ll K$, Eqn. 3 is very sensitive to \hat{v}_j , and only best-fit parameters will make significant contributions to p_i^N . The best-fit value of v_0 for a star without a planet is $v_0^* = \langle v_j \rangle$, where

$$\langle x \rangle \equiv \sum_j x_j \sigma_j^{-2} / \sum_j \sigma_j^{-2}. \quad (\text{A11})$$

For a star with a planet,

$$v_0^* = \frac{\langle v \rangle \langle g^2 \rangle - \langle vg \rangle \langle g \rangle}{\langle g^2 \rangle - \langle g \rangle^2}, \quad (\text{A12})$$

and the best-fit K is

$$K^* = \frac{\langle vg \rangle - \langle v \rangle \langle g \rangle}{\langle g^2 \rangle - \langle g \rangle^2}. \quad (\text{A13})$$

Each possible orbit is weighted by a prior for planet mass distribution and a prior for orbital inclination (the latter is simply $\sin i$). However, for a given K , M_* , e and P_K , Eqn. A7 inversely relates M_p to a unique value of $\sin i$. Thus a marginalization over both parameters collapses to a single integral over inclination. For a power-law mass distribution with index α

$$\tilde{p} = C \int_0^{\pi/2} di \int_{M_1}^{M_2} \frac{dM_p}{M_p} \left(\frac{M_p}{M_1} \right)^\alpha \sin i = C \int_0^{\pi/2} di \left(\frac{M_p \sin i}{M_1} \right)^\alpha (\sin i)^{-\alpha} \cos i \quad (\text{A14})$$

where the normalization constant $C = -\alpha [1 - (M_1/M_2)^{-\alpha}]$ and M_1 and M_2 are the lower and upper bounds to the mass range. Equation A14 evaluates to:

$$\tilde{p} = \frac{-\alpha}{1 - \alpha} \frac{M_p \sin i}{M_1} \frac{1 - (M_1/M_2)^{1-\alpha}}{1 - (M_1/M_2)^{-\alpha}}. \quad (\text{A15})$$

The lower bound M_1 is either $0.3M_J$ (the mass of Saturn) or $M_p \sin i$, whichever is larger, and $M_2 = 13M_J$, the approximate limit for deuterium burning in brown dwarfs. $M_p \sin i$ is uniquely determined by K^* , M_* , e and P_K . We adopt $\alpha = -0.31$ based on Cumming et al. (2008).

Equation A15 is substituted into Eqn. A5 and marginalized over $\omega \in [0, 2\pi]$, $t_0 \in [0, P_K]$, and $e \in [0, 1]$. The first two are uniformly distributed, and the third is assumed to be distributed according to a Rayleigh function with a mean value of 0.225 (Moorhead et al. 2011). The only remaining parameter is orbital period P_K . We marginalize p_i^N over values of P_K drawn from a distribution $P_1 < P_K < P_2$ in a manner that reproduces a power-law distribution with index $\beta = 0.26$ (Cumming et al. 2008), with $P_1 = 1.7$ d and $P_2 = 245$ d. For better sampling of the best-fit values of P_K , we iteratively re-calculate this set of orbital periods using the Keplerian orbital fitting code RVLIN (Wright & Howard 2009), holding other parameters fixed to their best-fit values, and iterating three times. We normalize the values of p_i^N such that $p_i^0 + p_i^1 = 1$, and then evaluate the likelihood distribution of f using Eqn. A3.

REFERENCES

- Allard, F., Homeier, D., & Freytag, B. 2011, in *Astronomical Society of the Pacific Conference Series*, Vol. 448, 16th Cambridge Workshop on Cool Stars, Stellar Systems, and the Sun, ed. C. Johns-Krull, M. K. Browning, & A. A. West, 91
- Alsubai, K. A., et al. 2011, *MNRAS*, 417, 709
- Apps, K., et al. 2010, *PASP*, 122, 156
- Artigau, É., Donati, J.-F., & Delfosse, X. 2011, in *Astronomical Society of the Pacific Conference Series*, Vol. 448, 16th Cambridge Workshop on Cool Stars, Stellar Systems, and the Sun, ed. C. Johns-Krull, M. K. Browning, & A. A. West, 771
- Bailer-Jones, C. A. L. 2011, *MNRAS*, 411, 435
- Bakos, G. Á., Hartman, J. D., Torres, G., Kovács, G., Noyes, R. W., Latham, D. W., Sasselov, D. D., & Béky, B. 2011a, in *European Physical Journal Web of Conferences*, Vol. 11, European Physical Journal Web of Conferences, 1002
- Bakos, G. Á., et al. 2011b, *ApJ*, 742, 116
- Baraffe, I., Chabrier, G., Allard, F., & Hauschildt, P. H. 1998, *A&A*, 337, 403
- Barry, R., et al. 2011, in *Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series*, Vol. 8151, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series
- Batalha, N. M., et al. 2010, *ApJ*, 713, L109
- Bonavita, M., & Desidera, S. 2007, *A&A*, 468, 721
- Bonfils, X., et al. 2013, *A&A*, 549, A109
- Boyajian, T. S., et al. 2012, *Astrophys. J.*, 757, 112
- Cassan, A., et al. 2012, *Nature*, 481, 167
- Christian, D. J., et al. 2009, *MNRAS*, 392, 1585
- Cumming, A., Butler, R. P., Marcy, G. W., Vogt, S. S., Wright, J. T., & Fischer, D. A. 2008, *PASP*, 120, 531
- de Bruijne, J. H. J. 2012, *Ap&SS*, 341, 31
- Deming, D., et al. 2009, *PASP*, 121, 952
- Dotter, A., Chaboyer, B., Jevremović, D., Kostov, V., Baron, E., & Ferguson, J. W. 2008, *ApJS*, 178, 89
- Feroz, F., Balan, S. T., & Hobson, M. P. 2011, *MNRAS*, 416, L104
- Fischer, D. A., & Valenti, J. 2005, *ApJ*, 622, 1102
- Fischer, D. A., et al. 2012, *ApJ*, 745, 21
- Fressin, F., et al. 2013, *ApJ*, 766, 81
- Fukugita, M., Ichikawa, T., Gunn, J. E., Doi, M., Shimasaku, K., & Schneider, D. P. 1996, *AJ*, 111, 1748
- Gaidos, E. 2013, *ArXiv e-prints* 1301.2384
- Gaidos, E., Fischer, D. A., Mann, A. W., & Lépine, S. 2012, *ApJ*, 746, 36
- Gaidos, E., & Mann, A. W. 2013, *ApJ*, 762, 41
- Gillon, M., et al. 2012, *A&A*, 542, A4
- Girardi, L., et al. 2012, *TRILEGAL*, a TRIdimensional model of the GALaxy: Status and Future, ed. A. Miglio, J. Montalbán, & A. Noels, 165
- Gray, R. O., & Corbally, C. J. 2009, *Stellar spectral classification, Princeton series in astrophysics* (Princeton, NJ: Princeton Univ. Press)
- Gray, R. O., Corbally, C. J., Garrison, R. F., McFadden, M. T., Bubar, E. J., McGahee, C. E., O'Donoghue, A. A., & Knox, E. R. 2006, *AJ*, 132, 161
- Hébrard, G., et al. 2010, *A&A*, 512, A46
- . 2013, *A&A*, 549, A134
- Hellier, C., et al. 2011, *A&A*, 535, L7
- Henry, T. J., & McCarthy, Jr., D. W. 1993, *AJ*, 106, 773
- Howard, A. W., et al. 2010, *Science*, 330, 653
- . 2012, *ApJS*, 201, 15
- Isaacson, H., & Fischer, D. 2010, *ApJ*, 725, 875
- Johnson, J. A., Aller, K. M., Howard, A. W., & Crepp, J. R. 2010, *PASP*, 122, 905
- Johnson, J. L., & Li, H. 2012, *ApJ*, 751, 81
- Kaib, N. A., Raymond, S. N., & Duncan, M. 2013, *Nature*, 493, 381
- Kokubo, E., Kominami, J., & Ida, S. 2006, *ApJ*, 642, 1131
- Lantz, B., et al. 2004, in *Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series*, Vol. 5249, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, ed. L. Mazuray, P. J. Rogers, & R. Wartmann, 146–155
- Laughlin, G., Bodenheimer, P., & Adams, F. C. 2004, *ApJ*, 612, L73
- Lépine, S., Hilton, E. J., Mann, A. W., Wilde, M., Rojas-Ayala, B., Cruz, K. L., & Gaidos, E. 2013, *AJ*, 145, 102
- Lissauer, J. J., & Stevenson, D. J. 2007, *Protostars and Planets V*, 591
- Lo Curto, G., et al. 2010, *A&A*, 512, A48
- Lovis, C., et al. 2011, *ArXiv e-prints* 1107.5325
- Mann, A. W., Gaidos, E., & Gaudi, B. S. 2010, *ApJ*, 719, 1454
- Mann, A. W., Gaidos, E., Kraus, A., & Hilton, E. J. 2013, *ArXiv e-prints* 1304.7269
- Mann, A. W., Gaidos, E., Lépine, S., & Hilton, E. J. 2012, *ApJ*, 753, 90
- Moorhead, A. V., et al. 2011, *ApJS*, 197, 1
- Moutou, C., et al. 2005, *A&A*, 439, 367
- . 2009, *A&A*, 496, 513
- . 2011, *A&A*, 527, A63
- Naef, D., Mayor, M., Beuzit, J.-L., Perrier, C., Queloz, D., Sivan, J.-P., & Udry, S. 2005, in *ESA Special Publication*, Vol. 560, 13th Cambridge Workshop on Cool Stars, Stellar Systems and the Sun, ed. F. Favata, G. A. J. Hussain, & B. Battick, 833
- Neves, V., Bonfils, X., Santos, N. C., Delfosse, X., Forveille, T., Allard, F., & Udry, S. 2013, *A&A*, 551, A36
- Penny, M. T., et al. 2012, *ArXiv e-prints* 1206.5296
- Pepe, F., et al. 2011, *A&A*, 534, A58
- Quirrenbach, A., et al. 2012, in *Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series*, Vol. 8446, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series
- Schneider, J., Dedieu, C., Le Sidaner, P., Savalle, R., & Zolotukhin, I. 2011, *A&A*, 532, A79
- Ségransan, D., et al. 2011, *A&A*, 535, A54
- Shen, Y., & Turner, E. L. 2008, *ApJ*, 685, 553
- Strohmer, T. 2000, *SIAM J. Sci. Comput.*, 22, 1160
- Thébault, P., Marzari, F., & Scholl, H. 2006, *Icarus*, 183, 193
- Torres, G., Fischer, D. A., Sozzetti, A., Buchhave, L. A., Winn, J. N., Holman, M. J., & Carter, J. A. 2012, *ApJ*, 757, 161
- Triard, A. H. M. J., et al. 2013, *MNRAS*, in press
- Udry, S., Fischer, D., & Queloz, D. 2007, *Protostars and Planets V*, 685
- Valenti, J., & Piskunov, N. 1996, *Astronomy and Astrophysics Supplement Series*, 118, 595
- Vogt, S., et al. 1994, in *Proc. SPIE Instrumentation in Astronomy VIII*, ed. D. L. Crawford & E. R. Craine (SPIE), 362
- Williams, J. P., & Cieza, L. A. 2011, *ARA&A*, 49, 67
- Wittenmyer, R. A., Tinney, C. G., O'Toole, S. J., Jones, H. R. A., Butler, R. P., Carter, B. D., & Bailey, J. 2011, *ApJ*, 727, 102
- Wright, J., Marcy, G., Howard, A., Johnson, J. A., Morton, T., & Fischer, D. A. 2012, *Astrophys. J.*, 753, 160
- Wright, J. T., & Howard, A. W. 2009, *ApJS*, 182, 205
- Wright, J. T., et al. 2011, *PASP*, 123, 412

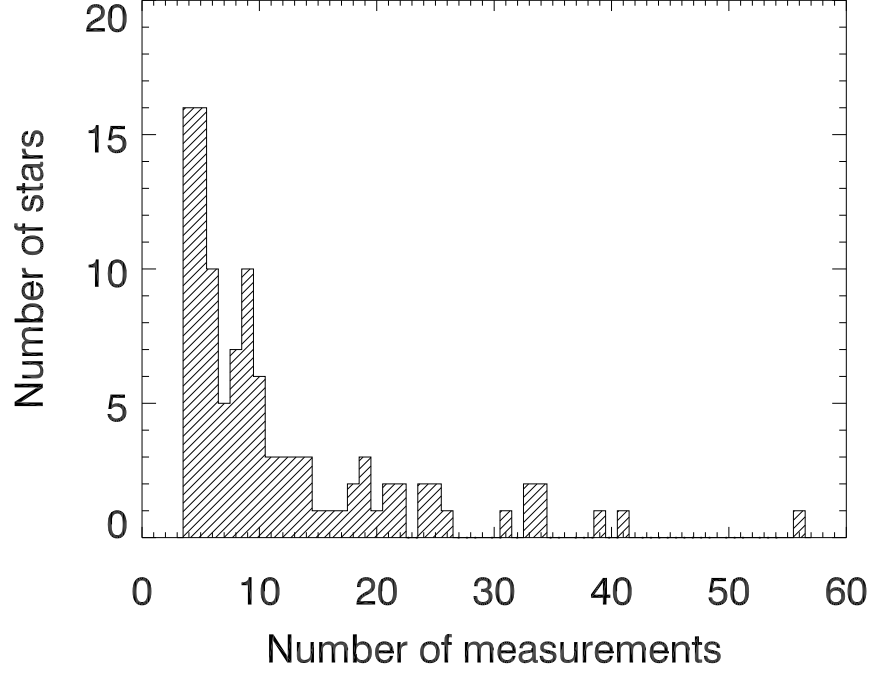


Figure 1. Distribution of number of Doppler measurements per star for those M2K stars selected for the analysis of giant planet fraction. One star (HIP 57274) with two giant planets has 120 observations and is off scale.

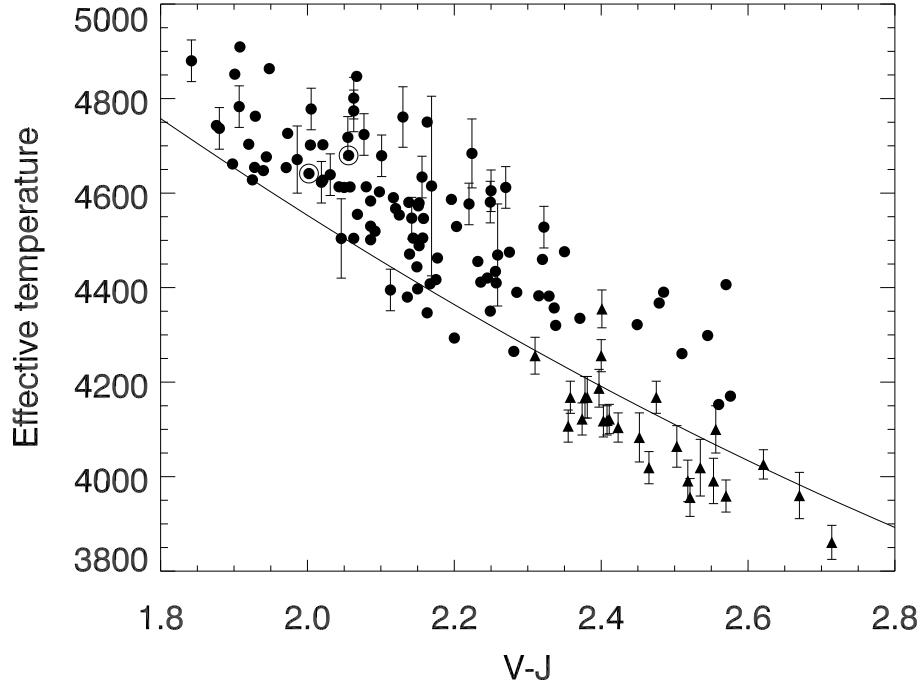


Figure 2. Stellar effective temperature vs. $V-J$ color of late K dwarfs in the M2K Doppler survey. Circles represent temperatures from SME analyses of high-resolution spectra (Valenti & Piskunov 1996), whereas triangles represent temperatures from fitting medium-resolution spectra to PHOENIX synthetic spectra (Mann et al., in prep) and calibrating on stars in Boyajian et al. (2012). Only some error bars are shown for clarity. The solid curve is an empirical T_{eff} vs. $V-J$ relation from Boyajian et al. (2012). Two systems with published giant planets (HIP 57274 and HIP 2247) are circled.

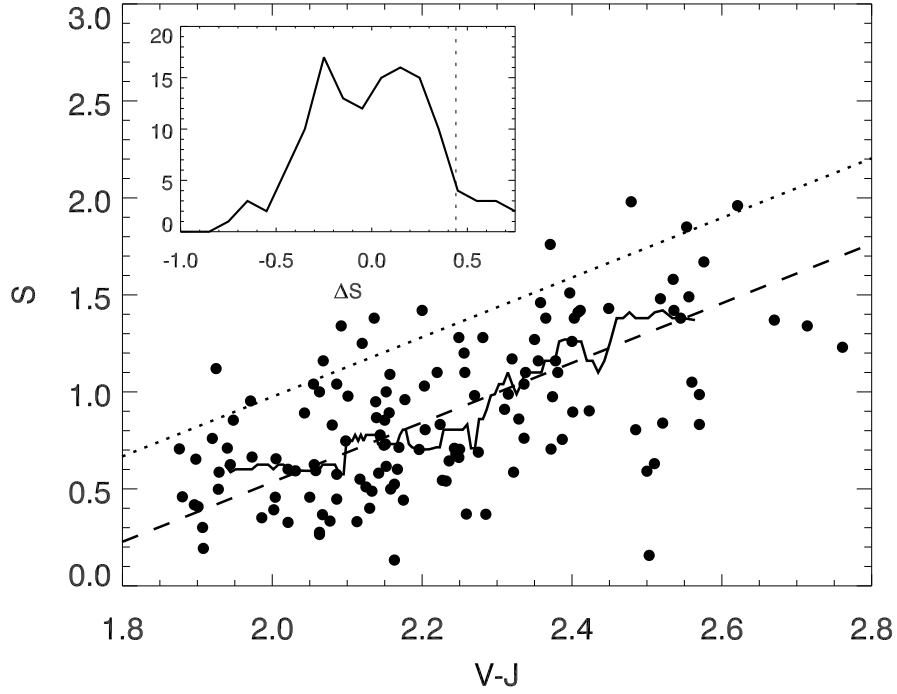


Figure 3. Flux S in the core of the Ca II HK lines, normalized by the continuum, vs. V - J color. High values of S are associated with elevated stellar activity and astrophysical Doppler noise or “jitter”. The solid line is a running median ($N = 20$), the dashed line is a linear regression of the median \bar{S} , and the dotted line is the linear fit $+ 0.44$, above which stars were excluded from the analysis. This threshold was selected based on the distribution of $\Delta S = S - \bar{S}$ (inset). Eleven stars or 8% of the sample were excluded based on this criterion.

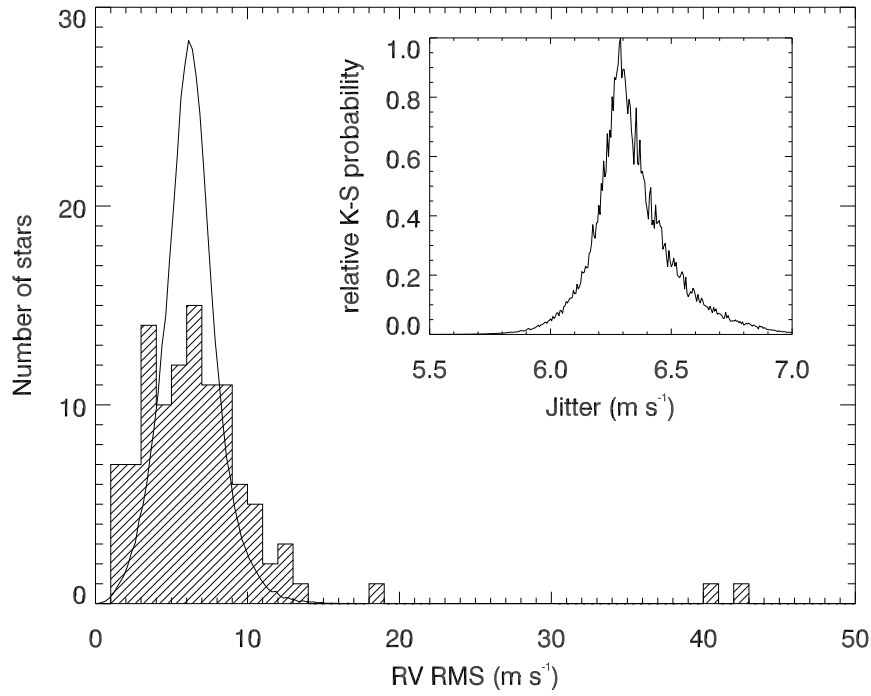


Figure 4. Distribution of adjusted radial velocity RMS among 110 M2K stars after excluding or adjusting case of high RMS. One star with $\text{RMS} = 65 \text{ m s}^{-1}$ falls outside the plot. Systems with $\text{RMS} > 15 \text{ m s}^{-1}$ were either excluded or significant linear/quadratic trends fitted and removed (see text). The solid curve is the best-fit model for the resulting distribution at $\text{RMS} < 15 \text{ m s}^{-1}$ assuming pure Gaussian-distributed noise that is the sum of formal errors and an astrophysical noise term σ_0 that includes both stellar jitter and barycenter motion due to small planets. The value $\sigma_0 = 6.3 \text{ m s}^{-1}$ which best reproduces the observed distribution was selected by maximizing the Kolmogorov-Smirnov statistic that the actual and model RMS values are drawn from the same distribution (inset).

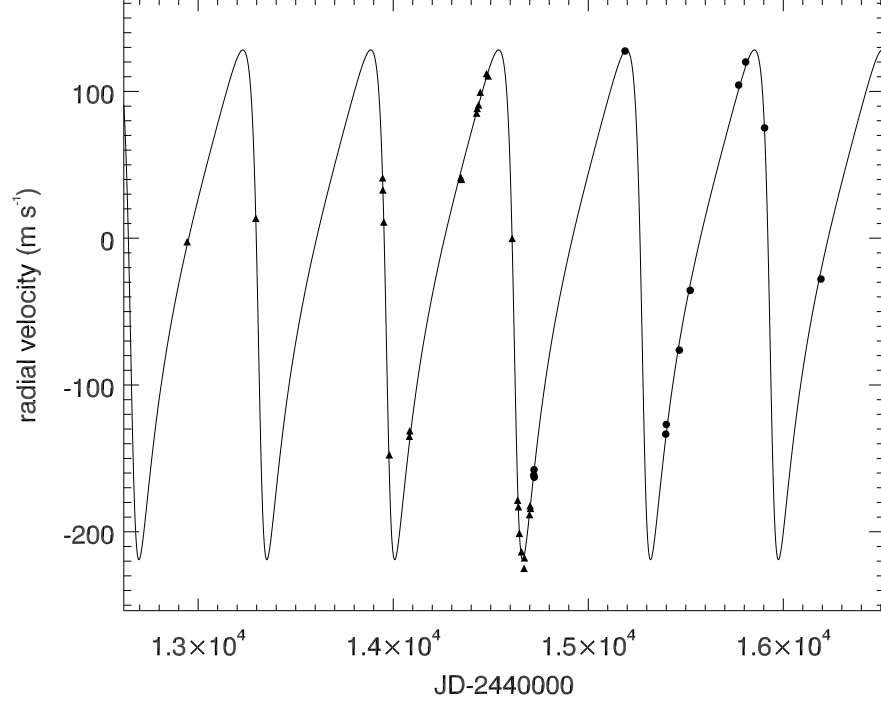


Figure 5. Thirty-eight radial velocities of HIP 2247 showing barycenter motion produced by the long-period giant planet discovered by Moutou et al. (2009). Triangles are Moutou et al. measurements with HARPS and circles are M2K measurements with Keck-HIRES. The solid line is the best-fit Keplerian orbit with $m \sin i = 5.14 M_J$, $P_K = 655.9$ d, and $e = 0.543$.

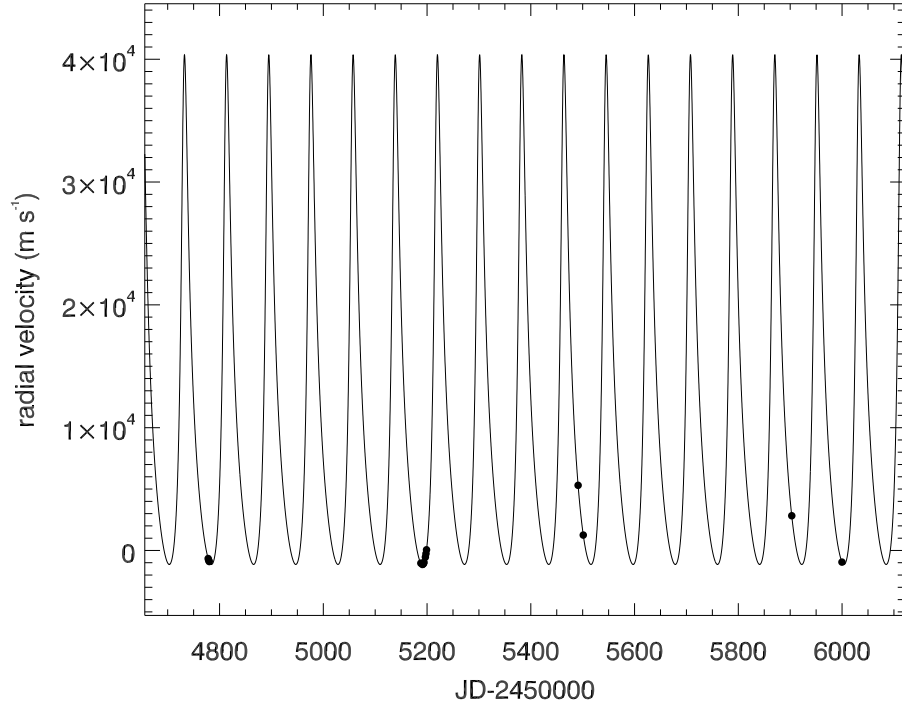


Figure 6. Fifteen M2K radial velocities of the the K+M binary star system HIP 38117. The best-fit Keplerian orbit has $P_K = 81.28$ d and $e = 0.478$.

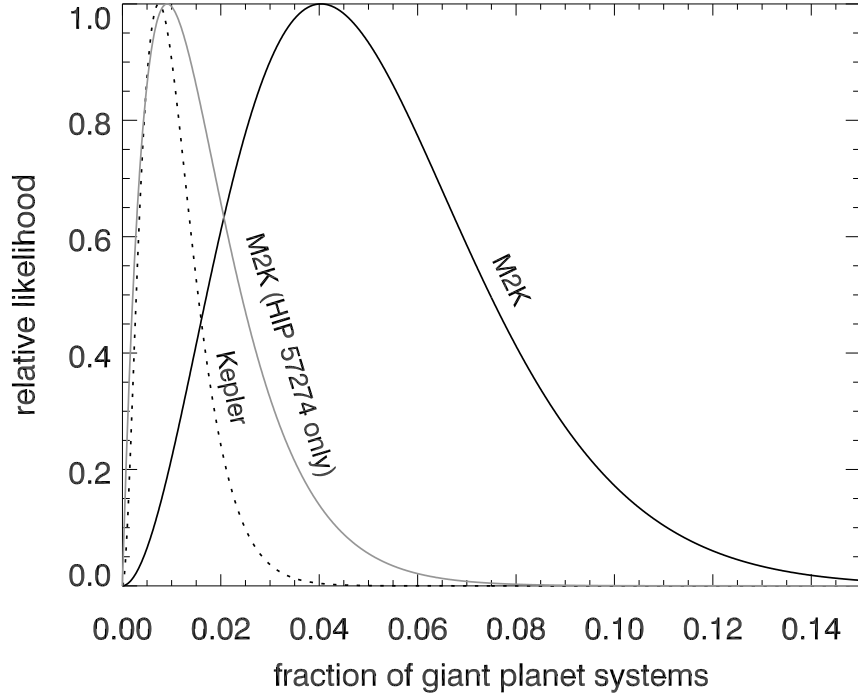


Figure 7. Probability distribution of the fraction of 110 M2K stars with giant planets with $M_p > 0.3M_J$ and $P_K < 245$ d (solid curves). The curve labeled “HIP 57274 only” assumes that such planets are ruled out around all but one of the stars: HIP 57274. The dashed line is the probability distribution of the fraction of *Kepler* late K dwarfs having giant planets with $0.7R_J < R_p < 2R_J$ and $P_K < 245$ d.

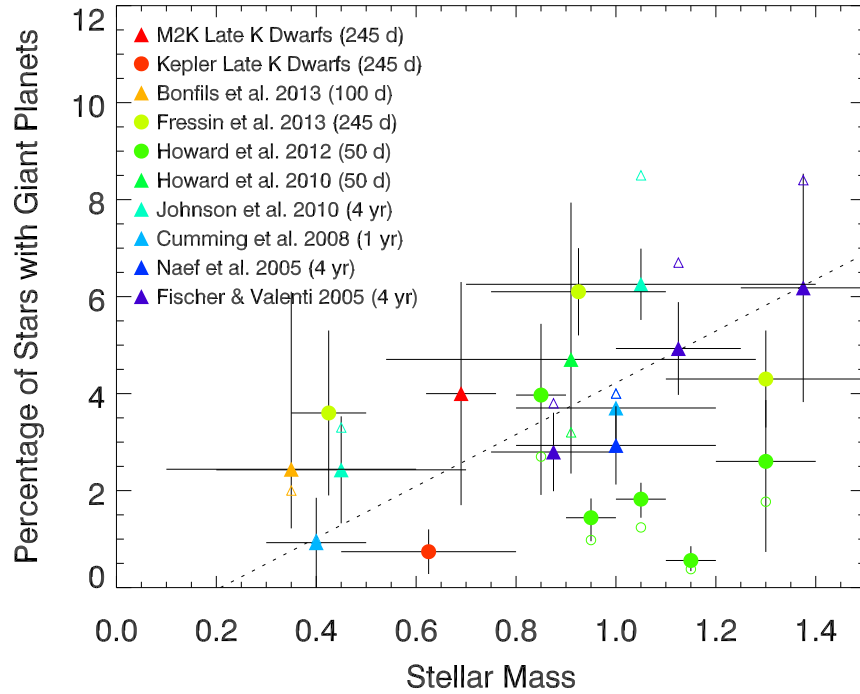


Figure 8. Adjusted percentage of stars with giant planets (Saturn mass or greater) vs. stellar mass. Points are color-coded according to their source and the symbol indicates whether the estimate is based on a RV (triangles) or transit (circles) survey. Each estimate was adjusted by the factor $\ln(P_{max}/1.7 \text{ d})/\ln(245/1.7)$ to account for different choices of maximum orbital period P_{max} (see legend). The unadjusted values are plotted as smaller open symbols of the same type and color. The range of stellar masses is in some cases approximate. The dashed line is a linear least-squares fit to the adjusted Doppler estimates.

Table 1
Confirmed Giant Planets around Mid- and Late-K-type Dwarf Stars^a

Planet	Mass (M_J)	Period (d)	SpT	$B - V$	T_{eff}	References
WASP-80b	0.55	3.068	K7-M0	0.94	~ 4000	Triaud et al. (2013)
HIP 70849 ^b	> 3	> 5 yr	K7	1.42	4100 ^c	Ségransan et al. (2011)
WASP-43b	2.03	0.813	K7	1.0	4400 ^d	Hellier et al. (2011)
HAT-P-20b	7.25	2.88	K3	—	4619	Bakos et al. (2011b); Torres et al. (2012)
HIP 57274c	0.41 ^e	32.0	K4	1.11	4640	Fischer et al. (2012)
HIP 57274d	0.53 ^e	431.7				
WASP-59b	0.0.86	7.92	K5	0.92	4650 ^h	Hébrard et al. (2013)
HD 113538b	0.27 ^e	263.3	K9 ^f	1.38	4685	Moutou et al. (2011)
HD 113585c	0.71 ^e	1657				
HIP 2247b	5.12 ^e	655.6	K4	1.14	4714	Moutou et al. (2009)
WASP-10b	3.06	3.09	K5	—	4735	Christian et al. (2009); Torres et al. (2012)
BD -08 2823b	0.33	237.6	K3	1.07	4746	Hébrard et al. (2010)
HD 20868b	1.99	380.85	K3/4	1.04	4795	Moutou et al. (2009)
HD 63454b	0.38 ^e	2.82	K4	1.06	4840	Moutou et al. (2005)
Qatar-1b	1.09	1.42	N/A	1.06	4861	Alsubai et al. (2011)
HIP 5158b ^g	1.44 ^e	345.6	K5	1.08	4962	Lo Curto et al. (2010)

^a $M_p \sin i > 0.3 M_J$ and K dwarf hosts with spectral subtypes 4 or later in the Exoplanet Catalog (Schneider et al. 2011) or $1 < B - V < 1.5$ in the Exoplanets Data Explorer (Wright et al. 2011)

^b Incomplete orbit and parameters are poorly constrained.

^c Based on infrared photometry and the temperature-luminosity relation of Baraffe et al. (1998)

^d T_{eff} based on $H\alpha$ and may need to be revised upward based on new mass estimate (Gillon et al. 2012)

^e $M_P \sin i$

^f Stellar parameters are problematic: Gray et al. (2006) assigns it the unrecognized spectral type K9, and its $B - V$ and $V - J$ colors suggest a star at the K-M spectral type boundary. Gray et al. (2006) also assign it a “k” to indicate interstellar absorption features, seemingly inconsistent for a star only 16 pc away. Moutou et al. (2011) and Bailer-Jones (2011) assign T_{eff} of 4685 K and 4625 K based on spectra and photometry, respectively. To reconcile the T_{eff} and colors, Bailer-Jones (2011) estimate ~ 1 mag of extinction, also inconsistent with its proximity.

^g This system also includes HIP 5185c, which may be a brown dwarf (Feroz et al. 2011).

^h T_{eff} was estimated by the null dependence of abundance on excitation potential.

Table 2
Stars Included in the Analysis

Name	$V-J$	T_{eff} (K)	[Fe/H]	S	M (M_{\odot})	N_{obs}	RMS (m s $^{-1}$)	p^1
HIP 1078	2.13	4426 ^b	—	0.49	0.75	4	2.56	0.005
HIP 1532	2.52	3956 ^a	-0.37	0.84	0.64	24	4.28	0.011
HIP 2247	2.06	4680	0.24	0.62	0.77	12	0.00	0.000
HIP 3418	2.16	4546	0.02	0.50	0.73	5	1.54	0.004
HIP 4353	2.20	4587	0.17	0.70	0.77	6	12.89	0.961
HIP 4454	1.99	4671	-0.55	0.35	0.71	5	3.62	0.004
HIP 4845	2.58	4170	-0.19	1.67	0.63	33	3.55	0.005
HIP 5247	2.51	4260	-0.22	0.63	0.66	12	7.76	0.052
HIP 5663	2.34	4357	-0.05	1.04	0.68	24	0.00	0.000
HIP 6344	2.32	4383	-0.04	0.99	0.68	5	1.71	0.007
HIP 9788	2.15	4444	-0.37	0.73	0.67	17	4.53	0.008
HIP 10337	2.54	4019 ^a	0.12	1.58	0.66	22	7.74	0.019
HIP 10416	1.88	4743	0.14	0.71	0.76	11	10.43	0.721
HIP 11000	1.92	4703	0.20	0.76	0.73	13	10.54	0.195
HIP 12493	2.25	4350	-0.29	0.66	0.68	6	4.50	0.032
HIP 13375	2.50	4110 ^b	0.00	0.59	0.56	9	3.68	0.010
HIP 14729	2.15	4579	0.17	1.00	0.70	10	5.76 ^c	0.007
HIP 15095	2.28	4265	-0.21	1.28	0.68	10	6.82	0.071
HIP 15563	2.06	4718	0.16	1.04	0.72	12	10.74	0.332
HIP 15673	1.93	4654	-0.46	0.50	0.69	6	3.12	0.007
1234-00069-1	1.90	4522 ^a	—	0.42	0.75	4	1.30	0.023
HIP 17346	2.06	4613	0.07	0.59	0.74	6	4.19	0.012
HIP 17496	2.15	4489	-0.04	0.62	0.72	5	2.53	0.008
HIP 19165	2.24	4412	-0.22	0.64	0.65	31	5.16	0.010
HIP 19981	2.25	4605	0.27	0.70	0.77	5	4.60	0.017
HIP 20359	2.14	4547	-0.04	0.58	0.75	5	4.47	0.011
HIP 25220	2.04	4613	0.05	0.89	0.71	10	7.92	0.049
HIP 26196	2.34	4245 ^b	—	0.76	0.74	8	4.26 ^d	0.012
4356-01014-1	1.88	4737	-0.17	0.46	0.77	8	2.69	0.003
HIP 29548	2.32	4528	-0.10	0.59	0.69	20	3.79	0.006
HIP 30112	2.36	4168 ^a	—	1.46	0.72	25	7.45	0.040
HIP 30979	2.02	4627	0.23	0.60	0.77	12	5.41	0.005
3388-01009-1	2.36	4220 ^b	—	1.38	0.68	10	64.66	0.500
HIP 32769	2.24	4420	-0.05	0.68	0.71	16	4.86	0.005
HIP 32919	2.33	4382	-0.01	0.86	0.70	18	5.29	0.006
1352-01588-1	2.31	4270 ^b	—	0.00	0.69	7	18.27	0.918
0748-01711-1	2.50	4064 ^a	—	0.16	0.66	25	42.28 ^c	0.500
HIP 36551	2.09	4501	-0.30	0.57	0.70	11	3.86	0.007
HIP 37798	2.54	4082 ^b	—	1.42	0.70	9	3.12	0.005
HIP 38969	2.13	4761	0.26	0.40	0.81	10	10.96 ^c	0.817
HIP 40375	2.18	4463	0.03	0.96	0.71	33	6.67	0.009
HIP 40671	2.05	4612	0.06	0.46	0.74	6	1.95	0.008
HIP 40910	2.41	4119 ^a	-0.06	1.41	0.68	21	9.47	0.665
HIP 41130	2.26	4410	-0.10	1.10	0.72	18	8.46	0.603
HIP 41443	2.08	4613	0.01	0.83	0.74	9	6.10	0.014
HIP 42567	1.94	4648	0.09	0.71	0.76	6	6.00	0.037
HIP 43534	2.56	4100 ^a	-0.13	1.49	0.64	14	6.88	0.006
HIP 43667	2.12	4554	0.01	0.51	0.72	9	5.24	0.020
HIP 44072	2.16	4347	-0.42	0.52	0.71	5	3.96	0.020
HIP 45042	2.35	4476	0.17	1.27	0.73	5	9.94	0.095
1955-00658-1	2.52	3991 ^a	0.21	1.48	0.66	4	6.05	0.055
HIP 45839	2.12	4590	0.05	0.55	0.72	5	12.40	0.865
HIP 46343	2.20	4529	0.03	1.03	0.70	10	4.35	0.008
HIP 46417	2.28	4475	-0.06	0.69	0.71	9	7.19	0.018
HIP 47201	2.37	4122 ^a	0.03	0.98	0.69	7	4.91	0.045
HIP 48139	2.09	4548 ^a	0.22	0.45	0.77	6	2.34	0.004
HIP 48411	2.14	4505	0.20	0.78	0.73	4	8.32	0.057
HIP 48740	2.22	4577	0.02	1.10	0.72	8	7.38	0.015
HIP 50960	2.40	4187 ^a	-0.06	1.51	0.65	8	8.22	0.023
HIP 51443	2.16	4505	-0.05	1.09	0.71	19	8.56	0.447
HIP 53327	2.29	4390	-0.79	0.37	0.66	4	5.13	0.018
HIP 54459	2.26	4469	-0.52	0.37	0.68	13	8.32	0.028
HIP 54651	2.11	4395	-0.89	0.33	0.66	6	1.63	0.002
HIP 54810	2.09	4256 ^a	0.03	1.04	0.70	5	6.18	0.061
HIP 55507	2.42	4104 ^a	-0.05	0.90	0.69	22	6.37 ^c	0.013
HIP 56630	2.67	3960 ^a	-0.01	1.37	0.68	9	7.29	0.045
HIP 57274	2.00	4641	0.08	0.39	0.76	120	0.00	1.000
HIP 57493	2.38	4168 ^a	0.06	1.16	0.71	15	5.48	0.009
HIP 59496	2.41	4122 ^a	-0.01	1.42	0.69	7	9.67	0.203
HIP 60633	2.08	4724	0.25	0.33	0.76	26	12.92	1.000
HIP 62406	2.38	4168 ^a	0.31	1.10	0.68	39	8.07	0.118
HIP 62847	1.97	4726	0.05	0.66	0.81	34	6.03	0.012
HIP 63894	2.20	4361 ^b	—	0.81	0.69	8	6.47	0.029
HIP 64048	2.17	4615	0.08	0.71	0.71	14	8.63	0.029
HIP 64262	2.03	4639	-0.25	0.59	0.70	9	8.13	0.047
HIP 66074	2.32	4460	0.23	1.17	0.73	9	11.06	0.818
HIP 66222	2.71	3861 ^a	-0.11	1.34	0.68	13	6.54	0.017
HIP 66283	1.84	4880	0.18	0.00	0.84	7	10.71	0.256
HIP 66840	2.47	4019 ^a	—	0.00	0.69	5	1.96	0.008
HIP 67842	2.76	3919 ^b	—	1.23	0.64	6	5.18	0.016